

Decision Tree Analysis to Identify Harmful Contingencies and Estimate Blackout Indices for Predicting System Vulnerability

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Abstract

Cascading failure is the main mechanism for progressing large blackouts in power systems. Following an initial event, it is challenging to predict whether there is a potential for starting cascading failure. In fact, the potential of an event for starting a cascading failure depends on many factors such as network structure, system operating point and nature of the event. In this paper, based on the application of decision tree, a new approach is proposed for identifying harmful line outages with the potential of starting and propagating cascading failures. For this purpose, associated with each trajectory of the cascading failure, a blackout index is defined that determines the potential of the initial event for triggering cascading failures towards power system blackout. In order to estimate the blackout indices associated with a line outage, a three stages harmful estimator decision tree (HEDT) is proposed. The proposed HEDT works based on the online operating data provided by a wide area monitoring system (WAMS). The New England 39-bus test system is utilized to show the worthiness of the proposed algorithm.

Keywords: Blackout; cascading failure; decision tree; harmful line outage.

31 **1. Introduction**

32 Security assessment with respect to critical contingency with the potential for triggering
33 cascading failure leading to blackout is the main concern for complex modern power systems.
34 Cascading failure is recognized as one of the major threats for a blackout in power systems.
35 Cascading failures successively weaken the system and make further failures more likely so that
36 a blackout can propagate to disable large portions of the electric power system. The failure can
37 be due to a variety of means, including action or malfunction of the protection system, automatic
38 or manual controls, and physical breakdown. Long, intricate cascades of events were the main
39 cause of the August 2003 blackout in Northeastern America that disconnected 61,800 MW of
40 power [1], and cascading failures from Germany to eastern Europe resulted in Europe blackout
41 in 2006 [2].

42 Typical contingency analysis based on the n-1 security is not able to reveal system vulnerability
43 and harmful contingencies with the potential for developing blackout. Therefore, a blackout
44 based security assessment is necessary for revealing harmful contingencies and vulnerable
45 operating conditions. For this purpose, simulation of the cascading failure is a vital requirement.
46 However, the process of cascading failure is very complex and time consuming to be
47 implemented in the context of a contingency analysis algorithm.

48 There are two approaches for modeling dynamic of cascading events and blackout in power
49 systems. The first one is deterministic approaches in which each component is modeled in detail.
50 Complete dynamical description of power system involves detailed knowledge of each
51 component and its coupling to the rest of the system. Because all of the components and the
52 physical laws governing their interactions are known, the simulation of the process for cascading
53 blackouts and events would be possible. The second one is probabilistic approaches in which

54 events and process of cascading events and blackout are probabilistically modeled based on the
55 random characteristic of the events [3].

56 DC load flow analysis is an approximate method for the determination of static flows within a
57 power system. The method is useful due to the fact that it produces approximate flows in a
58 system with a linear non-iterative method. This is in comparison to the use of AC load flow
59 analysis which makes use of iterative procedures, such as the Gauss-Seidel and Newton-Raphson
60 methods, in order to find solutions [4], [5]. The DC load flow analysis is less accurate than a full
61 AC load flow due to the fact that it is based on assumptions. These assumptions give good
62 approximations to the flow distributions that occur after contingencies and therefore the large
63 increase in the tractability, and a number of cascading events that can be analyzed, make the DC
64 load flow approximation a useful tool in cascading failure modeling for power systems. In [6], a
65 modified DC power flow-based cascading failure simulator to evaluate its utilization in the
66 contingencies triggered by both bus and branch failures is presented in which simulation results
67 of DC are compared and validated against the transient stability analysis based approach. In [7],
68 by using “DC” load flow and analysis of hidden failures of the network, the blackout is modeled.
69 In [8], the effect of the choice of DCOPF solution at each stage on the risk of cascading failures
70 is shown. Using DC power flow, Ref. [9] proposes an open source MATLAB based package for
71 academic purposes to analyze cascading failures due to line overloads in a power grid.

72 In Ref. [10] a variety of methods are emerged to study the mechanism of cascading outages, and
73 the theory can be divided into four categories: self-organized criticality, complex network theory,
74 operational reliability theory, power system simulation theory. Carreras et al. have produced
75 comprehensive work on self-organized criticality [11]-[13] in cascading failures using the AC
76 power flow-based Manchester model [14], [15] and CASCADE model [16]. In [17], transmission

77 grid reliability concerning cascading line overloads and outages is studied. In [18] the system
78 reliability of the cascading models is analyzed. In [19] angle stability of power system with
79 multiple operating conditions considering cascading failure is proposed. In [20], a new method in
80 detecting power system islanding contingencies using both the system's topological structure and
81 real-time system dynamic state variables is presented. A probabilistic framework for online
82 identification of post fault dynamic behavior of power systems with renewable generation based
83 on decision trees is introduced in [21]. In [22], illustrates how complex network theory can be
84 applied to modern smart grids in structural vulnerability assessment, cascading blackouts, grid
85 synchronization, network reconfigurations, distributed droop control, pinning control for micro-
86 grid autonomous operations, and effective grid expansions. In [23], a decision tree assisted
87 scheme is presented to determine the timing of controlled islanding in real time by using phasor
88 measurements. The objective of [24] is to develop adaptive controlled islanding as a component
89 of an emergency power system control strategy. In [25], a unified framework is proposed to
90 clarify the important concepts related to DSE, forecasting-aided state estimation, tracking state
91 estimation, and static state estimation.

92 While a wide variety of models are proposed for modeling blackouts, but to the authors'
93 knowledge, rare studies are done in the prediction of blackouts. It demonstrates the importance
94 of this paper. For instance, in Ref. [26] the stochastic processes in the dynamics of cascading
95 failure propagations in power systems is studied which can provide predictive information for
96 the failure spreading in the network. Ref. [27] proposes a probabilistic approach for prediction of
97 cascading failure in power system, which predicts the next transmission line to trip based on the
98 initial triggering event by considering the thermal limit of each line as a constraint.

99 The present research proposes a new method for identifying critical line contingency with the

100 potential for developing cascading failure propelling power system toward blackout. This new
101 approach is based on the Decision Tree Analysis. In this approach, at the pre-contingency steady
102 state condition by online measurement of the active power of line by means of WAMS, the
103 proposed DT is able to evaluate the harmfulness of the line outage for triggering cascading
104 failure and blackout. The proposed method is based on the static model in which element
105 overloading is considered as the main cause for creating and developing cascaded events.
106 Finally, based on IEEE 39-bus test system, the simulations are conducted to demonstrate the
107 effectiveness of the proposed model.

108 The rest sections of this research are organized as follows: Cascading failure model is introduced
109 in Section II. In Section III, the structure of the proposed approach is described. The simulation
110 study of the research is done in Section IV. Finally, the relevant conclusions are included in
111 Section V.

112 **2. Cascading failure modeling**

113 The Cascading failure is one of the important mechanisms to develop the large blackouts in
114 power networks. The term “failure” indicates the outage of elements in power system due to the
115 action of protection devices to prevent damages to the components of the system. Following an
116 initial event, e.g., a fault or outage of a line with heavy loading, the system may experience some
117 violations like severe voltage drop, line overloading or generator swing. If these violations can
118 activate protective relays, the process of cascading failure will start and continue according to
119 system vulnerability. System potential for triggering and propagating cascading failures
120 following an initial event is referred as the risk of power networks for the blackout.

121 The cascading failure process can be propagated and triggered based on the following
122 characteristics of power networks.

- 123 1. Brittleness of system components (like a transmission line, transformer and generator)
124 due to limit violations following each event.
- 125 2. Activation of protective relays plays a key role to trigger new component outage leading
126 to propagation of cascading events.
- 127 3. The principal cause for bringing out new outage following an initial event is relay
128 tripping of violated elements. Thus, the limit violation by system components
129 accompanied by relay action is the prime reason for propagating cascading failure. On the
130 developed stages of cascading failures, undesirable islands can propel power system into
131 a blackout.

132 For modeling the phenomena of cascading failure in power systems, various methods and
133 algorithms are proposed. In the Following the main four methods are described.

134

135 **2.1. CASCADE model**

136 The CASCADE model is an analytically tractable model for general systems with the potential
137 of cascading failure [16]. This model does not incorporate the complicated nature of power
138 systems and the interactions of components within the system. It qualitatively describes the
139 nature of cascading events in power systems and therefore is an appropriate model to introduce
140 the concept of cascading failure in power transmission systems. The model comprises of a
141 system of n identical components with each given an independent random initial loading. Each
142 component has a loading failure threshold at which the component fails. After a component fails
143 it transfers a fixed amount of its load to the other components of the system. A disturbance has
144 occurred in the system which results in random increases in the loadings of the components. If
145 loading of any of the components goes above its threshold value it fails and its load will be

146 transferred to the remaining system components. The secondary increase due to the failed
147 component may cause more components to go above their threshold values which cause
148 cascading failure to propagate more. The cascade stops when all of the components are tripped
149 out or none of the components have a value above their threshold. This relatively simple model
150 captures the essence of cascading failures in power transmission systems.

151

152 **2.2. Hidden Failure Model**

153 The Hidden Failure model is based on the idea that cascading failure within power systems can
154 occur due to the failure of protective relays which are physically and electrically close to a
155 transmission line which has been forced out [28]. The hypothesis is that a line failure exposes a
156 hidden failure in the protective equipment of neighboring branches. If a line fails, its neighbors
157 are given a probability of failure that is a function of the new loading of the line. As a result of
158 this cascading mechanism, as each neighbor fails, the initial disturbance can propagate through
159 the system resulting in diminished transmission capacity and load shedding. This model while
160 diverging from the simpler CASCADE model, by including the transfers of loading in a manner
161 that is more consistent with power system operation, still shows characteristics that are close to
162 that of the CASCADE model

163

164 **2.3. The Manchester Model**

165 The Manchester model uses a full AC load flow analysis [29] to model cascading failures
166 through sympathetic tripping of components including generator instabilities in response to
167 disturbances with subsequent load shedding. It is again observed in this model that the risk of

168 blackouts goes through a critical phase transition in response to an increase in the system
169 loading.

170

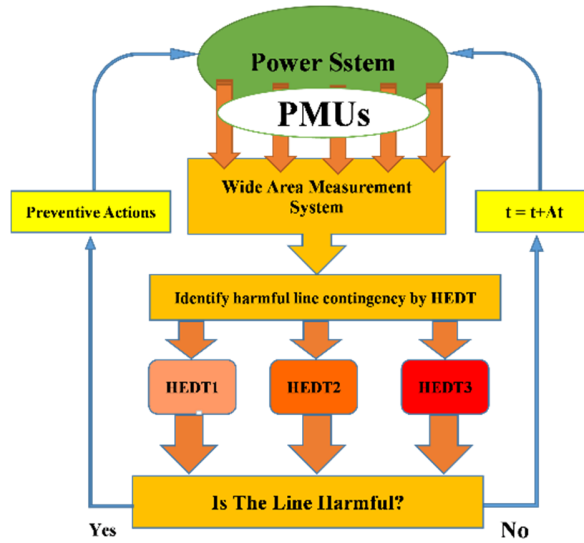
171 **2.4. OPA model**

172 All of the above models simulate the evolution of cascades through a system in the short term
173 and therefore model only is used for a given fixed topology, the full representation of real-world
174 power transmission systems would include the engineering response to blackouts or perceived
175 threats of blackout risk. The OPA model was developed to model this evolution of a power
176 system to a dynamical state that is near a critical point [30-31]. The model represents in a very
177 simplified manner the cascading dynamics of the electrical power transmission system, reduction
178 in the generation capacity of the power system as well as the operation, maintenance and repair
179 of the transmission system. These simplifications may lead to the behavior of the model to be
180 unable to represent the actual dynamics of power systems appropriately.

181

182 **3. The Proposed Approach**

183 The conceptual structure of the proposed algorithm for identifying harmful line contingency with
184 the potential for initiating and propagating cascading failures in power systems leading to
185 blackout is shown in Fig. 1.



186

187

Fig. 1. The conceptual structure of the proposed algorithm for identifying harmful line outage.

188

189

Based on the proposed approach, in a real-time environment, at any instant of system operation

190

by using operational data gathered by WAMS through the system, the harmfulness of each line

191

contingency for initiating cascading failure and propelling system to blackout is evaluated. For

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this purpose, a harmful estimator decision tree (HEDT) is designed and trained which can

193

estimate the harmfulness of each line outage for initiating cascading failure leading to a blackout.

194

The operational data required for HEDT consist of active power flow of lines which are

195

measured directly by PMUs. If a line contingency is recognized as harmful with the potential for

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developing cascading failure and blackout, so, it remains to adopt proper preventive actions as

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remedial actions to mitigate line hazardously.

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3.1. Cascading Failure simulation

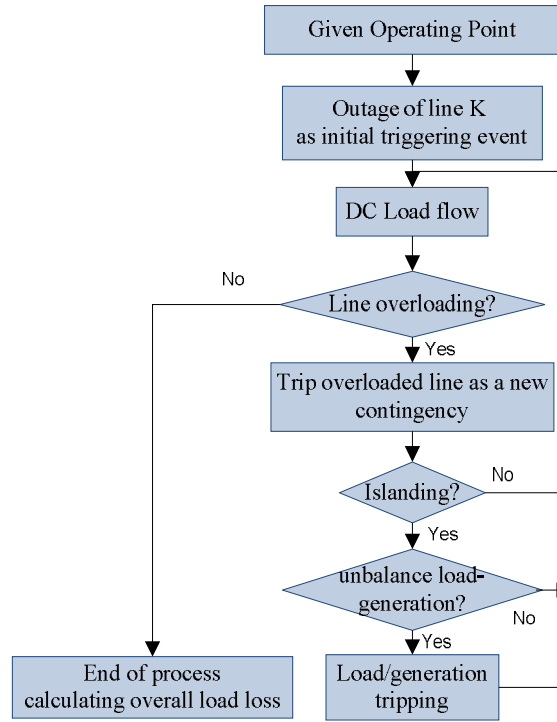
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In order to train harmful estimator decision tree (HEDT), it is required to prepare proper training

201

data including cascading failures trajectories with the potential for creating a blackout in power

202 system. Fig. 2 shows the process of the procedure used for evaluating blackout size associated
 203 with harmful cascading failures. The process can be explained in the following steps.



204
 205 Fig. 2. The process of blackout evaluation due to cascading failure following an initial event.

206
 207 **A. Step1: Initiating cascading failures**

208 The line outage, whose harmfulness for propagating cascading failure in the system is intended,
 209 is referred as the initial event. For all operating points with different network structures which
 210 are designed for training data preparation, the intended line is taken out as the initiating event,
 211 and its effect on the propagation of cascading failure in the system will be evaluated.

212 **B. Step2: Tripping overloaded lines**

213 Line tripping is one of the most general failures responsible for propagating cascading failures
 214 [4]. Each tripping element is referred to as a chain of the cascading failures, and the whole chain
 215 of the cascading failures following an initiating event leading to power system blackout is

216 denoted as a blackout trajectory. When the initial event occurs, it may cause overloading on
 217 some of the transmission lines. The protective relays are activated by overloading and trip
 218 dangerously overloaded lines. Tripping an overloaded line is regarded as a new cascaded event.
 219 In this paper, only line outages are considered as initial events. Tripping time of relays is not
 220 considered. Therefore, at each instant as soon as lines get overloaded, the line with the maximum
 221 overloading will be tripped immediately without any delay. System dynamic behavior and
 222 generator outage are not considered.

223 ***C. Step3: DC load flow***

224 In order to evaluate the change in line flow after each line outage, DC load flow is utilized which
 225 can be modeled as follows [5].

$$\begin{cases} P_{bus} = [A] \cdot \theta \\ P_{line} = [B] \cdot \theta \\ P_{line} = [B] \cdot [A]^{-1} \cdot P_{bus} \end{cases} \quad (1)$$

226 where θ is phase angle of bus voltages, P_{bus} is net injection power at buses, P_{line} is line active
 227 power flow, $[A]$ is reduced Jacobean matrix, $[B]$ is an incident matrix, B_{ij} is susceptance of
 228 the line connecting buses i and j.

229 Equations (1) can be written as (2):

$$\begin{aligned} P_{line} &= [C] \cdot P_{bus} \\ [C] &= [B] \cdot [A]^{-1} \end{aligned} \quad (2)$$

230

231 ***D. Step4: Islanding due to cascading Failure***

232 During the process of cascading failure, the initial network may be separated into several islands.
 233 Each island should be able to operate independently. In the case of unbalance load-generation the
 234 island may suffer from frequency or voltage instabilities, and it is necessary to shed excess

235 generation or load. The amount of load/generation trip is regarded as a criterion for measuring
236 criticality of the initial event.

237 238 **3.2. Blackout index**

239 In order to assess the harmfulness of the initial event, an index denoted as blackout index is
240 defined. According to this index, the potential of line outage for creating cascading failures
241 leading to blackout can be determined. Also one can rank the lines outage severity according to
242 their associated blackout indices. In this paper, the total power loss created due to cascading
243 failures following an outage of a line, is regarded as blackout index. It is worth noting that the
244 blackout index associated with each line contingency is strongly dependent on the system
245 operating condition and network structure.

246 In this paper, the technique of decision tree is used to evaluate the blackout index of each line
247 contingency according to the current operating condition. Equation (3) shows blackout index in
248 term of percentage of total load loss at the end of the process of cascading failure.

$$BI = \frac{P_{loss}}{P_{D_0}} \quad (3)$$

249 where P_{D_0} and P_{loss} are system initial load power and total loss respectively.

250 251 **3.3. Harmful Estimator Decision tree**

252 As it is mentioned, the harmfulness of a line contingency for initiating cascading failure and
253 blackout strongly depends on the system operating condition. Therefore the blackout index
254 associated with a line outage may vary in a wide range with respect to change in system
255 condition including load level, load-generation patterns and network structure. In this paper, in
256 order to have an online and fast estimator for evaluating the harmfulness of a line contingency,
257 the technique of decision tree is utilized in which by using online data acquired from WAMS,

258 harmfulness estimator decision trees HEDTs will predict the blackout indices of lines at the
259 current pre-contingency operating condition.

260 Noting that evaluating load curtailment and the number of islands, following the outage of a
261 critical line is possible only when the system has experienced the consequent of cascading
262 events. However, for evaluating the harmfulness of a line contingency, it is necessary to estimate
263 the consequent harmful results following the outage of the line in advance. The techniques of
264 artificial intelligence are very prone to such applications. They are usually trained based on the
265 offline data and then utilized in real time operational environment using online data.

266 In this paper, a three stages HEDT scheme is used for estimating harmfulness associated with
267 each line contingency. Fig. 3 shows the overall structure of the proposed three-stage HEDT
268 scheme. The proposed scheme uses pre-contingency lines active power flows and then estimates
269 the severity and harmfulness of each line contingency in term of the amount of power loss which
270 can be resulted due to cascading failure following the contingency. In fact, the proposed scheme
271 is able to estimate the potential of each line contingency for initiating cascading failure and
272 propelling system toward blackout. In order to simplify the training and estimating task of each
273 DT, the process of harmfulness estimation is divided into three stages. The input data for all DTs
274 is the active power flows of the line at the pre-contingency current operating point.
275 Corresponding to each line contingency, a specific estimation scheme shown in Fig. 3 is
276 designed and trained.

277 The first DT estimates whether following the outages of a line any blackout will occur or not. In
278 the case of any potential for creating blackout, the second and third DTs estimate the size of the
279 blackout in terms of MW loss. The classification of the harmfulness of the line contingency is
280 depicted in Table 1.

281

282 Table 1. The output of HEDTs for estimating harmful contingency

Harmfulness of line contingency	HEDT1	HEDT2	HEDT3	The size of the Associated blackout (MW)
safe	0	0	0	0
Partial blackout	1	0	0	>0 & <500
critical blackout	1	1	0	>500 & <1000
Large blackout	1	1	1	>1000

283
284

285 4. Simulation studies

286 In order to show the ability of the proposed algorithm for estimating harmfulness of line
287 contingency with the potential for triggering cascading failure and propelling the system toward
288 blackout; it is applied on IEEE 39 bus test system consisting of 46 transmission lines, ten
289 generating units and 19 load buses. In this study, the harmfulness of line #26 (bus16-bus17) is
290 supposed to be examined. Therefore, according to the proposed algorithm a 3 stage HEDT
291 scheme is trained to estimate harmfulness of line #26 as an initiating event for creating cascading
292 failure and developing blackout. It is worth noting that for estimating harmfulness of each line
293 contingency, an individual HEDT scheme is supposed to be trained.

294

295 4.1. Training data for HEDT

296 For training DTs of a HEDT scheme, proper training data should be provided. Provision of
297 training data needs a wide range of system operating conditions including a versatile range of
298 load level, load-generation pattern on buses. These operating conditions should contain different
299 degrees of vulnerability including harmful line contingencies and safe contingencies with no
300 potential for cascading failures and blackout. System base load is 6250 MW according to which,
301 five loading level as 80%, 90%, 100%, 105%, and 110% are examined.

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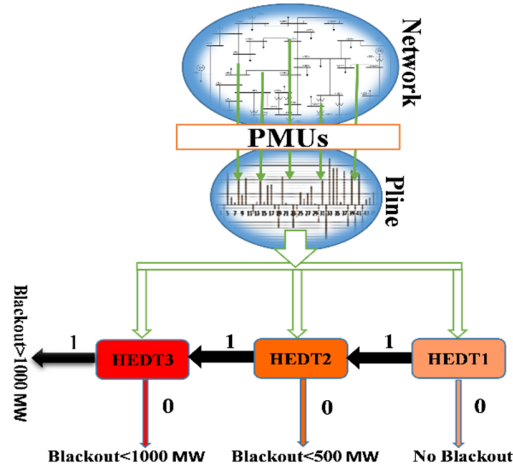


Fig. 3. Overall structure of the three stages HEDT scheme

303

304

305

306 Corresponding to each load level, there is a base load-generation pattern for which, around the
 307 corresponding base load-generation pattern, load and generation of all buses are changed
 308 randomly by $\pm 15\%$ by which 300 load-generation patterns are produced. In order to take into
 309 account the effect of network topology on the harmfulness of line contingencies, in addition to
 310 the basic structure of the network, single and double lines outage due to maintenance are
 311 considered in the network topology. In fact, by this way, the proposed HEDT will be robust with
 312 respect to topology change due to line maintenance. Table 2 shows the set of lines whose single
 313 and double outages are considered in the network topology. By combining these outages, as
 314 single or double outages, totally 90 different topology patterns are obtained.

315 Concerning each load-generation pattern, from 147 topology patterns, two maintenance patterns
 316 are adopted which resulted in total 600 operating scenarios from which 200 scenarios are for
 317 basic topology and 400 scenarios for maintenance topology with a versatile range of
 318 vulnerability from secure to worst cases. Pre-contingency steady state condition of each
 319 operating point is evaluated by power flow calculation.

Table 2. Lines whose outage are considered in the network topology.

No.	Line No.	Bus i	Bus j
1	1	1	2
2	3	2	3
3	6	3	4
4	7	3	18
5	8	4	5
6	9	4	14
7	11	5	8
8	15	7	8

320

321 **4.2. Calculation of blackout index**

322 With respect to the contingency of line #26 as the initial event whose harmfulness is intended to
 323 be evaluated by the proposed scheme, cascading failure simulation shown in Fig. 2 is performed
 324 for all operating scenarios. Corresponding to each operating scenario, the harmfulness of line
 325 #26 is evaluated. The active power flow of all lines at the pre-contingency steady state condition
 326 constitutes the input data for training HEDT associated to line #26, while the blackout (load loss)
 327 associated to the contingency of line #26 due to the cascading failure constitutes the output data
 328 of HEDT.

329 Table 3 shows a statistics overview of the harmfulness of line #26 within all 600 scenarios. As it
 330 can be seen, for example, 169 operating scenarios are within the load range 6000-6500 MW from
 331 which 69 scenarios are vulnerable concerning the contingency of line #26 as a harmful line.
 332 Total power loss associated with the outage of line #26 for all 69 vulnerable scenarios is 155453
 333 MW. The average power loss corresponding to each scenario is 919.8 MW as shown in the last
 334 row. As it can be seen, by increasing system load level mean blackout index is showing
 335 harmfulness of line #26 will increase.

336

337

338 Table 3. Statistic of harmfulness of line #26 in all scenarios

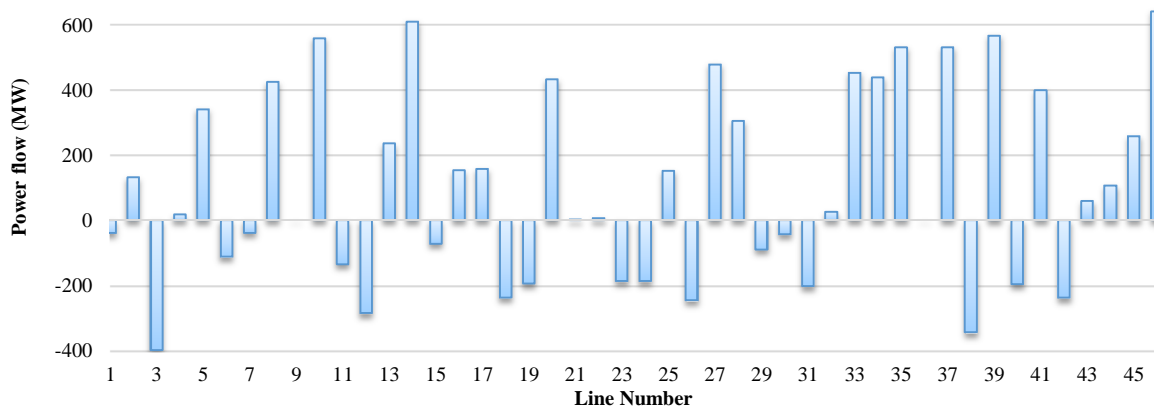
	Load level 1	Load level 2	Load level 3	Load level 4	Load level 5
Loading (MW)	<5500	5500-6000	6000-6500	6500-7000	>7000
No. of scenarios	130	145	169	115	41
Critical scenarios	41	62	69	56	18
%Critical scenarios	31.5%	42.8%	40.1%	48.7%	44%
Total blackout (MW)	72640	129430	155453	117048	43118
Mean blackout (MW)	558.8	892.6	919.8	1017.8	1051.7

339 Table 4 shows the sequence of cascading failures which are automatically triggered following
 340 the outage of line #26 as an initial event for a typical scenario (#261) in which system loading is
 341 5954 MW and line #9 (bus4-bus14) is out for maintenance. Blackout size associated with the
 342 contingency of line #26 at this scenario is evaluated to be 2239 MW.

343 Table 4. The sequence of cascading failures following an outage of line #26
 344

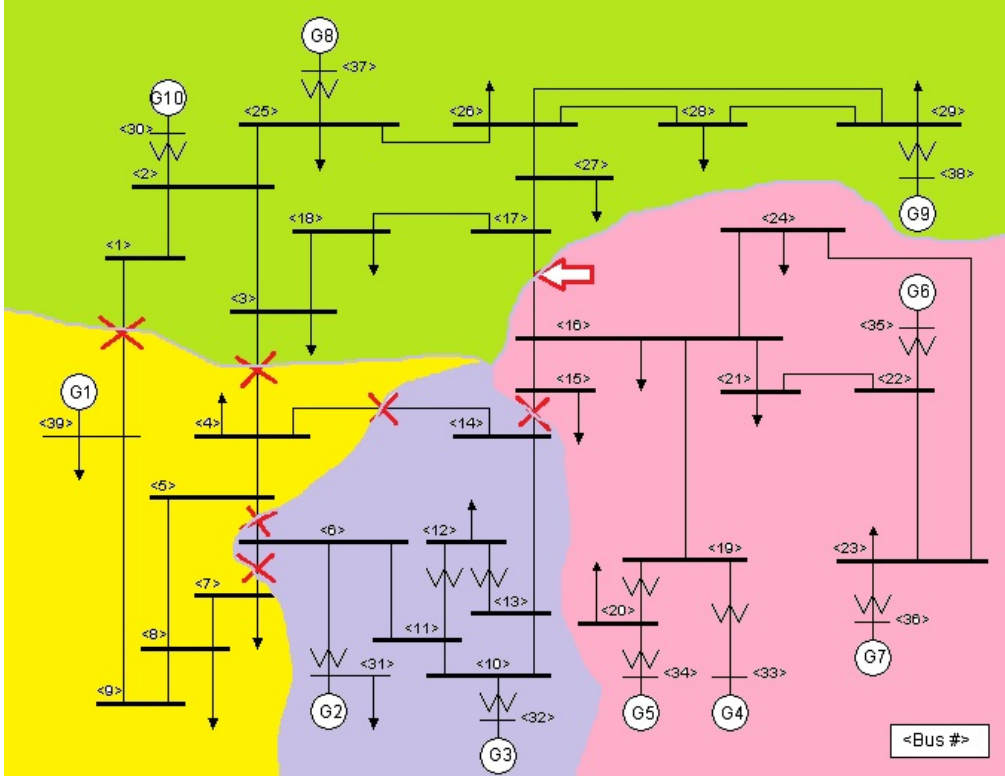
No.	Event type	Line Outage	Bus i	Bus j	Pline before outage (MW)
1	Initiating event	26	16	17	-247
2	1st cascaded failure	10	5	6	763
3	2nd cascaded failure	12	6	7	-1094
4	3rd cascaded failure	24	14	15	-629
5	4th cascaded failure	6	3	4	-570
6	5th cascaded failure	2	1	39	-608

345
 346 The pattern of line active power flow at the pre-contingency condition of this scenario which
 347 constitutes the input of HEDT is illustrated in Fig. 4.



348
 349 Fig. 4. Pattern of line active power flow for scenario #261

350 Fig. 5 shows islanding pattern created at the end of five cascading failures in Table 4. As it can
 351 be seen, the power grid is separated into four islands and finally after 2239 MW load loss, has
 352 been settled down in a new steady state condition.



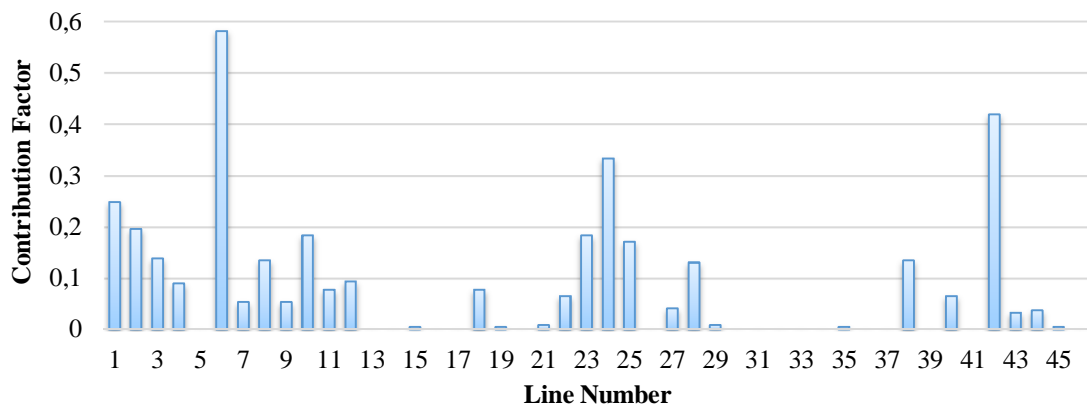
353
 354 Fig. 5. Islanding pattern due to cascading failures initiated by the contingency of line #26 at scenario #261

355
 356 Regarding all 246 vulnerable scenarios (out of 600), there are 246 corresponding blackout
 357 trajectories, each consisting of a chain of cascading failures. In order to rank the contribution of
 358 each line outage for participating in the chains of cascading failure, a contribution factor (CF)
 359 can be defined for each line #j as follows.

$$CF_j = \frac{NC_j}{N_{max}} \quad (4)$$

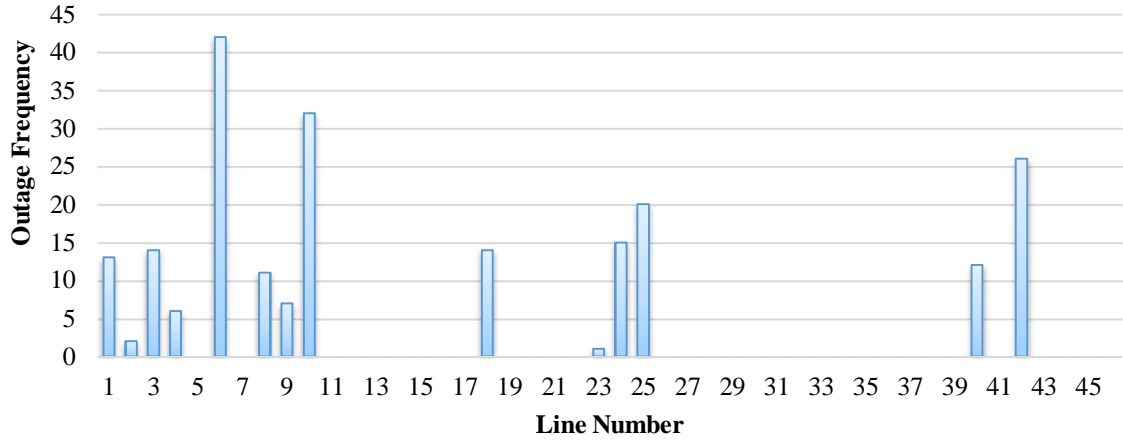
360 where NC_j is the total number of times which line #j has participated in all blackout trajectories
 361 as a chain of outages. N_{max} is the total number of blackout trajectories which is here 246.

362 The contribution factor of a line shows the number of times whose trip participates in the chains
 363 of cascading failures. As big as CF of a line, it will become more critical for propagating
 364 cascading failures following the initial outage of line #26. Fig. 7. shows the contribution factor
 365 of each line for participating in the cascading failures of 246 blackout trajectories following an
 366 outage of line #26 as initiating the event.



367
 368 Fig. 6. Contribution factor of lines for participating in cascading failures within 246 blackout trajectories triggering
 369 by the outage of line #26 as the initial event

370
 371 Fig. 7 shows a number of times by which each line trip has participated in the chain of cascading
 372 failure of all blackout trajectories as the first cascaded outage. For example, the trip to line #6
 373 (bus3-bus4) has participated 42 times out of 246 blackout trajectories as the first cascaded outage
 374 after the initial outage of line #26. So, the line #6 can be regarded as a critical line for
 375 propagating blackout through the network.



376

377 Fig. 7. Frequency of lines trip as the 1st cascaded event within 589 blackout trajectories following the initial outage
 378 of line #26

379 4.3. Input vector of HEDT

380 The input vector of each DT of the proposed HEDT scheme consists of lines active power flow
 381 at the pre-contingency condition as shown in Fig. 4 for a sample scenario. This vector can be
 382 prepared online using data from WAMS. The negative value shows a reverse direction of power
 383 on the line.

$$\underline{P} = [P_{L1}, P_{L2}, \dots, P_{Li}, \dots, P_{L46}] \quad (4)$$

384 where P_{Li} is the active power of line #i.

385 The set of vectors of active power flow corresponding to different scenarios constitutes the input
 386 matrix [P] for training HEDT. The number of rows is equal to the number of training patterns.
 387 Each vector of active power flow corresponds to a particular operating condition of the power
 388 system.

389

390 4.4. Training HEDT

391 In the proposed scheme, the first HEDT1 is responsible just for detecting the potential of the
 392 blackout. The second HEDT2 classifies vulnerable scenarios with respect to smaller or bigger

393 than 500MW blackout, and the third HEDT3 classifies vulnerable scenarios concerning smaller
 394 or bigger than 1000MW blackout. All HEDTs are trained and tested by 60% and 40% of
 395 prepared scenarios respectively. The proposed HEDTs are trained based on top-down search
 396 method for data classification. In this method by starting from a root node, samples are classified
 397 by submitting a series of questions about the properties associated with the data. A node is
 398 bisected into two sub-branches on the basis of the feasible answers for its question. Table 5
 399 shows the training/test performance of HEDT1 in which from 360 training scenarios, 135
 400 scenarios experienced a blackout and perfect classification is achieved.

401

402 Table 5. Training/Test Performance of HEDT1

Blackout risk	Training			Test		
	No. of training scenarios	False learning	%correct learning	No. of test scenarios	False estimate	%Correct estimate
Vulnerable	135	0	100	142	0	100
Secure	225	0	100	98	0	100

403 Table 6 shows the training/test performance of HEDT2 in which from 600 scenarios, 136 and 86
 404 training and test scenarios respectively experienced blackout greater than 500 MW. The
 405 corresponding accuracy of training and test are %97.8 and %98.8 respectively.

406 Table 6. Training/Test Performance of HEDT2

Blackout risk (MW)	Training			Test		
	No. of training scenarios	False learning	%correct learning	No. of test scenarios	False estimate	%Correct estimate
<500	224	2	%99.1	154	2	%98.7
>500	136	3	%97.8	86	1	%98.8

407 Table 7 shows the training/test performance of HEDT3 in which from 600 scenarios, 114 and 74
 408 training and test scenarios respectively experienced blackout greater than 1000 MW. The
 409 corresponding accuracy of training and test are %98.2 and %98.6 respectively.

410 Table 7. Training/Test Performance of HEDT3

Blackout risk (MW)	No. of training scenarios	Training		No. of training scenarios	Test	
		False learning	%Correct learning		False estimate	%Correct estimate
<1000	246	3	%98.8	166	3	%98.2
>1000	114	2	%98.2	74	1	%98.6

411

412 5. Conclusion

413 In this paper, an approach for predicting system vulnerability with respect to an outage of a line
 414 with the potential for cascading failures was established in the decision tree theory. In fact, the
 415 proposed scheme was able to estimate the potential of each line contingency for initiating
 416 cascading failure and propelling system toward blackout. A three stages HEDT scheme was used
 417 for estimating the harmfulness associated with each line contingency. DC power flow was used
 418 for modeling cascading failures. The procured results revealed that the proposed method was a
 419 powerful technique for online identification of critical branches. A large collection of system
 420 operating conditions including a versatile range of load level, load-generation pattern on buses
 421 was used for decision tree construction. The capability of the proposed algorithm was assessed
 422 through a 39-bus test system. The proposed decision tree was a valuable technique that was
 423 deemed robust under topological changes. The one of the most interesting topics for future work
 424 would be to develop precise models for blackout problem.

425

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